

AD-A181 129

TRANSVERSE KELVIN-HELMHOLTZ INSTABILITY WITH PARALLEL
ELECTRON DYNAMICS (U) SCIENCE APPLICATIONS
INTERNATIONAL CORP MCLEAN VA P SATYANARAYANA ET AL
28 MAY 87 NRL-MR-5960

1/1

UNCLASSIFIED

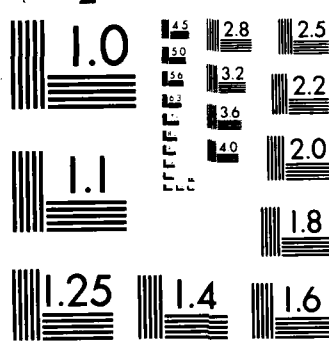
F/G 4/1

NL

FND

187

UIC



Naval Research Laboratory

Washington, DC 20375-5000



NRL Memorandum Report 5960

AD-A181 129

**Transverse Kelvin-Helmholtz Instability with Parallel
Electron Dynamics and Coulomb Collisions**

P. SATYANARAYANA,* Y. C. LEE,*† AND J. D. HUBA

*Geophysical and Plasma Dynamics Branch
Plasma Physics Division*

**Science Applications International Corporation
McLean, VA 22102*

*†University of Maryland
College Park, MD 20742*

May 20, 1987

DTIC
ELECTE
JUN 15 1987
S D

This research was partially sponsored by the Defense Nuclear Agency under work
unit code and title: 00158/Plasma Structure Evolution.

Approved for public release; distribution unlimited.

87 6 12 061

REPORT DOCUMENTATION PAGE

1a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED		1b. RESTRICTIVE MARKINGS	
2a. SECURITY CLASSIFICATION AUTHORITY		3. DISTRIBUTION/AVAILABILITY OF REPORT Approved for public release; distribution unlimited.	
2b. DECLASSIFICATION/DOWNGRADING SCHEDULE		5. MONITORING ORGANIZATION REPORT NUMBER(S)	
4. PERFORMING ORGANIZATION REPORT NUMBER(S) NRL Memorandum Report 5960		7a. NAME OF MONITORING ORGANIZATION	
6a. NAME OF PERFORMING ORGANIZATION Naval Research Laboratory	6b. OFFICE SYMBOL (If applicable) Code 4780	7b. ADDRESS (City, State, and ZIP Code)	
6c. ADDRESS (City, State, and ZIP Code) Washington, DC 20375-5000		9. PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER	
8a. NAME OF FUNDING/SPONSORING ORGANIZATION DNA and ONR	8b. OFFICE SYMBOL (If applicable)	10. SOURCE OF FUNDING NUMBERS	
8c. ADDRESS (City, State, and ZIP Code) DNA - Washington, DC 20305 ONR - 800 N. Quincy St., Arlington, VA 22203		PROGRAM ELEMENT NO. 61153N 62715H	PROJECT NO. RB-RC/ 02-44 00158
11. TITLE (Include Security Classification) Transverse Kelvin-Helmholtz Instability with Parallel Electron Dynamics and Coulomb Collisions			
12. PERSONAL AUTHOR(S) Satvanaravana, P., Lee, Y.C., and Huba, J.D.			
13a. TYPE OF REPORT Interim	13b. TIME COVERED FROM TO	14. DATE OF REPORT (Year, Month, Day) 1987 May 20	15. PAGE COUNT 32
16. SUPPLEMENTARY NOTATION This research was partially sponsored by the Defense Nuclear Agency under work unit code and title: 00158/Plasma Structure Evolution.			
17. COSATI CODES		18. SUBJECT TERMS (Continue on reverse if necessary and identify by block number)	
FIELD	GROUP	SUB-GROUP	
		> Kelvin-Helmholtz instability, High latitude ionosphere, Velocity shears.	
19. ABSTRACT (Continue on reverse if necessary and identify by block number) Electron parallel dynamics and Coulomb collisions are included in the analysis of the transverse Kelvin-Helmholtz instability. The electrons are treated kinetically while the ions are treated in the fluid limit. It is shown that, in the collisionless case, for an inhomogeneous velocity profile $V(x) = V_0 \tanh(x/L)$ the Kelvin-Helmholtz instability is stable for $k_z/k_y > (V_0/L \omega_{eh}) k_y L (1 - k_y^2 L^2)^{1/2}$ in the limit $\omega - k_y V_0 \gg k_z v_e$. Here, V_0 is the flow velocity, L is the scale length of the velocity shear layer, k_z and k_y are the parallel and perpendicular wavenumbers, respectively, $\omega_{eh} = (\Omega_e \Omega_i)^{1/2}$, and v_e is the electron thermal velocity. The stabilization of the mode is shown to be caused by the compressional energy given to the electrons parallel to \mathbf{B} . In the collisional limit, Coulomb collisions are shown to increase the unstable k_z domain because they inhibit the electron motion parallel to \mathbf{B} . Applications to the high latitude ionosphere are discussed.			
20. DISTRIBUTION/AVAILABILITY OF ABSTRACT <input checked="" type="checkbox"/> UNCLASSIFIED/UNLIMITED <input type="checkbox"/> SAME AS RPT <input type="checkbox"/> DTIC USERS		21. ABSTRACT SECURITY CLASSIFICATION UNCLASSIFIED	
22a. NAME OF RESPONSIBLE INDIVIDUAL J.D. Huba		22b. TELEPHONE (Include Area Code) (202) 767-3630	22c. OFFICE SYMBOL Code 4780

TABLE OF CONTENTS

	<u>Page No.</u>
I. INTRODUCTION.....	1
II. THEORY.....	2
III. COLLISIONLESS REGIME.....	3
(a) Analytical Results.....	3
(b) Numerical Results.....	4
(c) Energy Principle.....	7
IV. COLLISIONAL REGIME.....	8
V. SUMMARY AND DISCUSSION.....	9
ACKNOWLEDGMENTS.....	10
REFERENCES	10

Accession For	
NTIS CRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution /	
Availability Codes	
Dist	Avail and/or Special
A-1	



TRANSVERSE KELVIN-HELMHOLTZ INSTABILITY WITH PARALLEL ELECTRON DYNAMICS AND COULOMB COLLISIONS

I. INTRODUCTION

Velocity shear layers with steep gradient scale lengths are frequently observed in the high latitude auroral zone (Kelley and Carlson, 1982; Basu et al., 1985; Kelley and Earle, 1986). Recent HILAT satellite measurements reported by Basu et al. (1985) show flows with moderate to strong velocity shears with a shallow irregularity spectrum; often field aligned currents are also observed in the regions of sheared velocity flows. The observations suggest that the east-west $\mathbf{E} \times \mathbf{B}$ drift velocity, for example, is inhomogeneous and usually reverses its direction as one moves in the north-south direction. This kind of velocity shear transverse to the magnetic field is usually a source of Kelvin-Helmholtz instability (Chandrasekhar, 1961; Mikhailovskii, 1972). In the conventional Kelvin-Helmholtz instability the mixing of fluids with different velocities is confined to two dimensions transverse to the magnetic field; the ion polarization drift leads to the instability while the electrons simply $\mathbf{E} \times \mathbf{B}$ drift in the perpendicular plane. In the auroral ionosphere one cannot simply ignore the dynamics parallel to the magnetic field because there could be additional sources of free energy or damping that may affect the transverse mixing of the fluids with sheared velocity. Our aim is to introduce the third dimension into the two dimensional analysis of Kelvin-Helmholtz instability and, as a first step, we study the effects of parallel electron dynamics. Furthermore, since the electron parallel motion couples the collisionless and collisional regimes of the ionosphere, we also include Coulomb collisions between the electrons and ions. A preliminary analysis, in the collisionless domain, was performed by Thompson (1983) who showed that the parallel electron motion could have stabilizing influence on the Kelvin-Helmholtz instability. In this paper we perform (i) a more complete analysis and present a general

stability criterion for a specific velocity profile, (ii) present the effects of collisions on the instability. In analogy with the role of gravity on Kelvin-Helmholtz instability in neutral fluids, we observe that the parallel electron dynamics simulate buoyancy of a fluid in a gravitational field.

II. THEORY

We consider a homogeneous plasma that is drifting across a magnetic field ($\underline{B} = B \hat{z}$) because of an equilibrium inhomogeneous electric field ($\underline{E} = E_0(x) \hat{x}$). We choose $E_0(x) = E_0 \tanh(x/L)$ where L is the scale length of the shear layer. In this paper we restrict the analysis to the domain $L \gg \rho_i$ and $|\omega| \ll \Omega_i$, where ρ_i and Ω_i are the ion gyroradius and gyrofrequency, respectively. Incompressible plasma motion in two dimensions across an uniform magnetic field is determined by the constraint that the perpendicular current be divergence free,

$$\nabla \cdot \underline{j}_\perp = 0 \quad (1)$$

where $\underline{j}_\perp = ne(\underline{v}_{e\perp} - \underline{v}_{i\perp})$, e is the charge, n is the plasma density, $\underline{v}_{e\perp}$ and $\underline{v}_{i\perp}$ are the perpendicular drifts of electrons and ions. The velocities $\underline{v}_{e\perp}$ and $\underline{v}_{i\perp}$ are obtained from the momentum equations by assuming the electrons only $\underline{E} \times \underline{B}$ drift, while the ions experience both the $\underline{E} \times \underline{B}$ drift and the polarization drift. Linearizing (1) with a perturbed electrostatic potential of the form $\hat{\phi} \sim \hat{\phi}(x) \exp[-i(\omega t - k_y y)]$ with frequency ω and wavenumber k_y yields the equation governing the Kelvin-Helmholtz instability:

$$\frac{\partial^2 \hat{\phi}}{\partial x^2} + \left[-k_y^2 + \frac{k_y V_0''}{(\omega - k_y V_0)} \right] \hat{\phi} = 0 \quad (2)$$

where $V_0(x) = -(c/B)E_0(x)$. This is a well studied equation (Chandrasekhar, 1961; Mikhailovskii, 1964; Guzdar et al., 1982; Satyanarayana et al., 1983); instability ($\gamma > 0$, where γ is given by $\omega = \omega_r + i\gamma$) occurs in the wavenumber domain $0 < k_y L < 1$ for $V_0(x) = V_0 \tanh(x/L)$.

To extend the above theory to three dimensions, we need to consider the equation

$$\nabla_\perp \cdot \underline{j}_\perp = -\partial j_z / \partial z \quad (3)$$

which allows for a parallel current along the field lines. In this paper we consider perturbations along the magnetic field and also equilibrium currents along the field lines. We include electron collisions and use a BGK model to calculate the electron susceptibility (Clemmow and Dougherty, 1969). Kinetic treatment of the electron parallel motion yields a general equation for the perturbed electrostatic potential $\hat{\phi} = \hat{\phi}(x) \exp[-i(\omega t - k_z z - k_y y)]$ in the domain $|\omega|$ and $V_0/L \ll \Omega_i$

$$\frac{\partial^2 \hat{\phi}}{\partial x^2} + \left[-k_y^2 + \frac{k_y V_0''}{(\omega + i\nu_{in} - k_y V_0)} \right] \hat{\phi} - \frac{\omega_{lh}^2}{v_e^2} \left[\frac{1 + \xi_e Z(\xi_e)}{1 + i(v_e/k_z v_e) Z(\xi_e)} \right] \hat{\phi} = 0 \quad (4)$$

where $\omega_{lh}^2 = \Omega_e \Omega_i$, $\Omega_e(\Omega_i)$ is the electron (ion) gyro-frequency, v_e is the electron thermal velocity, $\xi_e = (\omega - k_y V_0 - k_z V_d + i\nu_e)/k_z v_e$, V_d is the equilibrium electron drift along the magnetic field, and ν_e is the electron collision frequency. For $\nu_e = 0$, (4) is the same as equation (8) of Thompson (1983) without the ion terms; we can ignore the parallel ion terms if we restrict our analysis to $\rho_i/L < 1$ where ρ_i is the ion gyroradius. We have introduced the parallel electron drift, V_d , and collisional effects which are absent in Thompson (1983).

III. COLLISIONLESS REGIME

(a) Analytical Results

In this section we set $\nu_e = 0$. A simple stability boundary defining the regions of k_z and k_y where the system is stable or unstable can be easily obtained in the domain where the electrons behave as a fluid; this is the region where the argument of the Z function is large (i.e., $|\xi_e| \gg 1$). In this domain the Z function can be approximated as $-1/\xi_e - 1/2 \xi_e^3$. With this approximation (4) takes the form

$$\frac{\partial^2 \hat{\phi}}{\partial x^2} + \left[-k_y^2 + \frac{k_y V_0''}{(\omega - k_y V_0)} + \frac{1}{2} \frac{k_z^2 \omega_{lh}^2}{(\omega - k_y V_0)^2} \right] \hat{\phi} = 0. \quad (5)$$

Equation (5) is identical to the Rayleigh equation governing the interchange of a drifting, weakly inhomogeneous fluid in a gravitational field with a sheared drift velocity (Drazin, 1958; Chandrasekhar, 1961). Here we identify the term $\omega_{lh}^2 k_z^2 / k_y^2$ with the buoyancy term that is driving the Rayleigh-Taylor instability g/L_n , where g is gravity and L_n is the density gradient scale length. In the spirit of the neutral fluid problem, we define a dimensionless number

$$J = \frac{1}{2} \frac{k_z^2}{k_y^2} \frac{L^2 \omega_{lh}^2}{V_0^2} . \quad (6)$$

Once we have made this identification, it follows that for $V_0(x) = V_0 \tanh(x/L)$ the stability boundary is simply (Drazin, 1958)

$$J = k_y^2 L^2 (1 - k_y^2 L^2) . \quad (7)$$

The modes are stable for $J > 1/4$ or

$$\frac{k_z^2}{k_y^2} > \frac{1}{2} \left(\frac{V_0}{L \omega_{lh}} \right)^2 . \quad (8)$$

Thus, parallel electron dynamics has a stabilizing influence on the Kelvin-Helmholtz instability.

Figure 1 shows the stability boundary where we plot J versus $k_y L$. We note that the conclusions of Thompson (1983) are qualitatively correct. However, our analysis shows that $J < 1/4$ for instability as opposed to $J < 1$ given by Thompson (1983) who did not consider the explicit shear profile $V(x) = V_0 \tanh(x/L)$. A derivation of this stability criterion based upon the energy principle is given in Sec. III.c.

(b) Numerical Results

We now solve (4) numerically to further show the effects of the parallel dynamics. In Figure 2 we plot the normalized growth rate $\gamma/(V_0 L)$ vs. $\alpha (= \omega_{lh}^2 L^2 / v_e^2)$ for $k_y L = 0.5$ (which gives maximum growth for $k_z = 0$), $k_z/k_y = 1.0 \times 10^{-3}$, $V_0/v_e = 0.01$, and $V_d = 0$. Curve A shows the growth rate for the collisionless case, while Curve B shows the growth rate when electron collisions are included (to be discussed in Sec. IV). For $\alpha = 0$ we find $\gamma/(V_0 L) = 0.19$ which is the usual result. As α is increased, we see the Kelvin-Helmholtz growth rate drops. Since for large α the Kelvin-Helmholtz term (i.e. $\propto V_0''$) does not contribute to (4), the mode equation essentially becomes

$$-k_y^2 v_e^2 - \alpha \omega_{lh}^2 [1 + \epsilon_e Z(\xi_e)] = 0 \quad (9)$$

which allows only stable roots in the fluid limit with $\omega_r = k_y V_0 = (1/2)(k_z/k_y)\omega_{lh}$. From Curve A of Figure 2 we also see that the modes are stable for $\alpha \geq 9$. This is in agreement with the criterion $J > 1/4$ previously discussed. We find that for reasonable values of the parallel drift velocity (i.e., $V_d < v_e$) these results are not significantly altered. We find that in this regime the argument of the Z function is large, indicating that the electrons are merely acting as a fluid and wave particle effects are not playing an important role. On the other hand, for sufficiently small α the theory breaks down as shown by the kink in Fig. 2; the orbits begin to play an important role here ($L \sim \rho_i$) and kinetic effects need to be included.

We now solve (4) for several mode numbers. Figure 3 shows the normalized growth rate $\gamma/(V_0 L)$ as a function of $k_y L$ for $V_0/v_e = 0.01$, $\alpha = 1$, and $k_z L = 0, 1.0 \times 10^{-3}, 2.0 \times 10^{-3}, 3.0 \times 10^{-3}$, and 4.0×10^{-3} as curves A, B, C, D and E, respectively. Curve A shows the conventional Kelvin-Helmholtz mode; $\gamma > 0$ in the wavenumber domain $0 < k_y L < 1$ and $\gamma_{\max} = 0.19$ for $k_y L = 0.46$. Several points are to be noted from this figure: (i) as $k_z L$ is increased the wavenumber of the maximally growing mode increases; for example, for $k_z L = 4.0 \times 10^{-3}$ the growth rate maximizes at $k_y L \sim 0.8$, (ii) the growth steadily decreases as $k_z L$ increases, dropping by 50% for $k_z L = 3 \times 10^{-3}$, and (iii) there is a narrower range of $k_y L$ for unstable modes; for $k_z L = 4.0 \times 10^{-3}$ the waves are unstable only in the region $0.60 < k_y L < 0.93$.

Equation (4) is solved both for the eigenvalues and the eigenfunctions (i.e., the perturbed electrostatic potentials). The eigenfunctions reveal some features of the stabilizing influence of the electron parallel motion. Briefly, the method used to solve (4) is the following: The asymptotic form of the solution is assumed to be WKBJ type

$$\hat{\phi}_\infty = \frac{1}{Q^{1/4}} \exp \left[- \int \sqrt{Q} dx \right]$$

where Q is the coefficient of $\hat{\phi}$ in (4). For a given value of $k_y L$, we search for an eigenvalue ω such that integration of (4) with $\hat{\phi}_\infty$ as the boundary condition yields a localized solution whose logarithmic

derivative $\partial/\partial x(\ln \hat{\phi})$ is continuous across, for example, the origin. We note that the electron terms are competing with $-k_y^2$ in (4) at $x = \infty$; if the electron terms are dominating Q at $x = \infty$ then Q could become positive, leading to oscillatory type solution at $x = \infty$. On the other hand, if the electron terms are not large such that Q at $x = \infty$ is negative, that is $-k_y^2$, the WKB solutions are exponentially decaying.

Figure 4 shows the solutions of (4) for $k_z L = 3.0 \times 10^{-3}$ and $k_y L = 0.7$ for which $\gamma/(V_0/L) = 0.09$ and $\omega_r/(V_0/L) = 0$. We see that both the real (A) and imaginary (B) parts are exponentially decaying at $x = \pm \infty$ and are fairly localized near the origin where the velocity reversal is taking place. The localization width is proportional to the thickness of the shear layer, $\Delta x \sim 4L$. The value of Q at $x = \infty$ is negative but greater than $-k_y^2 L^2$. In Figure 4b we show the full perturbed electrostatic potential, $\hat{\phi} \sim \hat{\phi}(x) \exp [ik_y y]$ using the wave function, $\hat{\phi}(x)$, for the maximally growing mode of Figure 4a. The dashed (solid) lines indicate the relative negative (positive) values of $\hat{\phi}$. We note that these values correspond to positive and negative vorticities of the fluid; the phase of $\hat{\phi}$ is such that it allows mixing of the fluid with different vorticities thereby causing the perturbation to grow.

In Figure 5 we show the eigenfunctions for the lower cutoff wavenumber $k_y L = 0.51$ corresponding to curve D of Fig. 3 for which $k_z L = 3.0 \times 10^{-3}$; the growth rate and the real frequency for this case are $\gamma/(V_0/L) = 0$ and $\omega_r/(V_0/L) = -0.057$, respectively. In this case we find that Q at $x = -\infty$ is positive showing oscillatory type solutions, while Q is negative at $x = \infty$ giving rise to an exponentially decaying solution. In comparison with Figure 4a, this figure shows that electrons are convecting energy away from the localized region in the shear layer, thus, leading to stabilization of the instability; this point is discussed in detail in the next section. In Figure 5b we show the corresponding $\hat{\phi}$. Comparison of Figs. 4b and 5b shows that the parallel motion of electrons changes the phase of $\hat{\phi}$ and the finite real frequency introduces a relative velocity to the wave preventing any mixing of the fluid in the $x < 0$ and $x > 0$ regions, thus causing the perturbation not to grow.

c. Energy Principle

In this section we present energy principle arguments to show the effects of electron parallel dynamics. The Kelvin-Helmholtz instability arises basically due to the conversion of available kinetic energy of relative motion of the equilibrium flow into wave energy. In this case the electrons are confined to the plane perpendicular to the magnetic field and only $\underline{E} \times \underline{B}$ drift. If we allow the electrons to move along the magnetic field, the available kinetic energy in the equilibrium flow has to overcome the parallel electron compressional energy for instability to occur.

We can quantify these arguments and obtain a stability condition as follows. We consider the interchange of two neighboring volume elements at x and $x + \delta x$ which are moving with velocities V_0 and $V_0 + \delta V$, respectively. The available kinetic energy is

$$\delta T = \frac{1}{2} n m_i [V_0^2 + (V_0 + \delta V)^2 - \frac{1}{2} (2V_0 + \delta V)^2] = \frac{1}{4} n m_i (\delta V)^2 \quad (10)$$

where m_i is the mass of the ions and n is the density. The compressional energy associated with fluid moving a distance δz (i.e., parallel to \underline{B}) is given by

$$\delta W = \left\langle \int_0^{\delta z} n m_e \delta \dot{v}_z dz \right\rangle = \frac{1}{2} n m_e \langle \delta \dot{v}_z \delta z \rangle \quad (11)$$

where m_e is the electron mass and

$$\delta \dot{v}_z = - (e/m_e) \partial \hat{\phi} / \partial z \quad (12)$$

and $\langle \quad \rangle$ denotes time averaged quantities. Since the perturbed electron motion in the perpendicular plane is predominantly $\underline{E} \times \underline{B}$ motion, we have

$$\delta v_x = - (c/B) \partial \hat{\phi} / \partial y . \quad (13)$$

From (12) and (13) we have

$$\frac{\delta v_x}{\delta v_z} = \frac{k_y}{k_z \Omega_e} \quad (14)$$

and

$$\frac{\delta x}{\delta v_z} = \frac{k_y}{k_z \Omega_e} \quad (15)$$

Substituting (14) in (11) we obtain

$$\delta W = \frac{1}{2} n m_e \left(\frac{k_z \Omega_e}{k_y} \right) \langle \delta z \delta v_x \rangle = \frac{1}{2} n m_e \left(\frac{k_z \Omega_e}{k_y} \right) \langle \delta x \delta v_z \rangle$$

from which the compressional energy is given as

$$\delta W = \frac{1}{2} n m_e \left(\frac{k_z \Omega_e}{k_y} \right)^2 (\delta x)^2 \quad (16)$$

From (10) and (16) the stability condition, $\delta T < \delta W$, is

$$\frac{1}{4} n m_i (\delta V)^2 < \frac{1}{2} n m_e \left(\frac{k_z \Omega_e}{k_y} \right)^2 (\delta x)^2 \quad (17)$$

or

$$\left(\frac{\partial V_0}{\partial x} \right)^2 < 2 (\Omega_e \Omega_i) (k_z^2 / k_y)^2 \quad (18)$$

since $\delta V = (\partial V_0 / \partial x) \delta x$. Thus, the stability condition can be written as

$$\frac{k_z^2}{k_y^2} > \frac{1}{2} \left(\frac{V_0}{L_{w2h}} \right)^2 \quad (19)$$

which agrees with (8) derived in Section II.

IV. COLLISIONAL REGIME

In this section we study the effects of electron collisions on the transverse Kelvin-Helmholtz instability. In Fig. 6 we plot the normalized growth rate $(\gamma / (V_0 / L))$ as a function of $k_z L$ for $V_1 = 0$, $V_0 / v_e = 0.01$, $k_z L = 1.0 \times 10^{-3}$, and $k_y L = 0.6$. The variation of the normalized growth rate for $v_e = 0$ is shown by curve A, and for $v_e = 100 (V_0 / L)$ by curve B. We note that the electron collisions introduce a new scale size, the collisional mean free path

$\lambda_{mfp} (= v_e/v_e)$. Since $\lambda_{mfp} \ll \lambda_z$, electron motion parallel to \underline{B} is inhibited, and as a consequence the $k_z L$ domain over which the modes are now unstable is much larger. This is shown clearly in Fig. 6, where the collisional growth rate (curve B) goes to zero for $k_z L > 0.07$, while the collisionless growth rate (curve A) drops to zero sharply for $k_z L > 0.005$.

In addition, curve B of Fig. 2 shows the collisional growth rate versus the coupling parameter α . For the range of α considered, electron collisions make the growth rate almost independent of α . The electron collisions thus have a destabilizing influence on Kelvin-Helmholtz instability. This would in turn alter the stability boundary in such a way that the basic Kelvin-Helmholtz mode is unstable in a larger k_z domain than the collisionless case.

V. SUMMARY AND DISCUSSION

In this paper we have considered the effect of parallel electron motion on the transverse Kelvin-Helmholtz instability as a first step toward a three-dimensional analysis of the nature of convective flows in the high latitude ionosphere. In the collisionless regime ($v_e = 0$), we show that for an inhomogeneous velocity profile given by $V(x) = V_0 \tanh(x/L)$ the Kelvin-Helmholtz instability is stable for $k_z/k_y > (V_0/L\omega_{eh})k_y L(1 - k_y^2 L^2)^{1/2}$ in the limit $\omega - k_y V_0 \gg k_z v_e$. We further show that the physical mechanism for stabilization is the compressional energy given to the electrons parallel to \underline{B} . In the collisional regime ($v_e \neq 0$), we show that the Kelvin-Helmholtz instability is not as easily stabilized by finite k_z effects; this is attributed to the inhibition of parallel electron motion for $\lambda_{mfp} \ll \lambda_z$.

We apply this stability criterion for parameters relevant to the high latitude ionosphere. We take $\omega_{eh} = 3.2 \times 10^4 \text{ sec}^{-1}$, $k_y L = 0.5$, and assume $k_z/k_y = (\sigma_{\perp}/\sigma_{\parallel})^{1/2}$ where σ_{\perp} and σ_{\parallel} are the perpendicular and parallel conductivities, respectively (Farley, 1959). The value of $\sigma_{\perp}/\sigma_{\parallel}$ varies with altitude in the ionosphere and is generally taken to be in the range 10^{-5} (lower F region) - 10^{-9} (topside F region). Thus, for instability to occur it is required that $V_0/L > 2.3 \text{ sec}^{-1}$ in the topside region. Velocity shears have been reported in the range $V_0/L = 0.5 - 20 \text{ Hz}$ (Kelley and Carlson, 1977; Earle and Kelley, 1966) so that the instability could locally be active in the topside F region. In the lower F region, where $\omega_{eh} = 10^2 - 10^3 \text{ sec}^{-1}$ and $V_0/v_e =$

10^{-2} velocity shears of order $1 - 10 \text{ sec}^{-1}$ are needed to drive the Kelvin-Helmholtz modes unstable (e.g., for $k_y L = 0.6$ and $k_z L = 0.01$). However, these conclusions are predicated on the important assumption that $k_z/k_y = (\sigma_{\perp}/\sigma_{\parallel})^{1/2}$ which may not be the case. Recent analyses of unstable flute modes in barium clouds (i.e., the gradient drift instability) (Sperling et al., 1984; Drake et al., 1985) indicate that $k_z/k_y \approx 0$ within the unstable cloud. A more detailed three-dimensional analysis (Drake and Huba, 1987) is needed to assess the role of the Kelvin-Helmholtz instability in high latitude dynamics. Finally, we add that we have neglected ion-neutral collisions in the analysis; these can be important in the lower F region. In a forthcoming study (Mitchell et al., 1987) we will present analytical and computational results demonstrating the effect of ion-neutral collisions on the transverse Kelvin-Helmholtz instability. In the linear regime, it is found that ion-neutral collisions have a stabilizing influence on the instability.

ACKNOWLEDGMENTS

This work is supported by the Defense Nuclear Agency and the Office of Naval Research.

REFERENCES

- Basu, S., S. Basu, C. Lenior, D. Weimer, E. Nielsen, and P.F. Fougere, Velocity shears and sub-km scale irregularities in the night time auroral F-region, Geophys. Res. Lett., **13**, 101, 1986.
- Chandrasekhar, S., Hydrodynamic and Hydromagnetic Stability, Clarendon, Oxford, 1961.
- Chaturvedi, P.K., J.D. Huba, S.L. Ossakow, and P. Satyanarayana, Parallel current effect on E-region plasma instabilities, submitted to J. Geophys. Res., 1986.
- Clemmow, P.C. and J.P. Dougherty, Electrodynamics of Particles and Plasmas, Addison-Wesley, Reading, 1969.
- Drake, J.F., J.D. Huba, and S.T. Zalesak, Finite temperature stabilization of the gradient drift instability in barium clouds, J. Geophys. Res., **90**, 5227, 1985.
- Drake, J.F. and J.D. Huba, Dynamics of three dimensional ionospheric plasma clouds, to be published in Phys. Rev. Lett., 1987.
- Drazin, P.G., The stability of a shear layer in an unbounded heterogeneous inviscid fluid, J. Fluid Mech., **4**, 214, 1958.

- Earle, G.D. and M.C. Kelley, Observations of velocity shear and waves associated with auroral arcs, EOS, 15, 336, 1986.
- Farley, D.T., Jr., A theory of electrostatic fields in a horizontally stratified ionosphere subject to a vertical magnetic field, J. Geophys. Res., 64, 1225, 1959.
- Gurnett, D.A. and L.A. Frank, Observed relation between electric fields and auroral particle precipitation, J. Geophys. Res., 78, 145, 1973.
- Guzdar, P.N., P. Satyanarayana, J.D. Huba, and S.L. Ossakow, Influence of velocity shear on the Rayleigh-Taylor instability, Geophys. Res. Lett., 9, 547, 1982.
- Kelley, M.C. and C.W. Carlson, Observations of intense velocity shear and associated electrostatic waves near an auroral arc, J. Geophys. Res., 82, 2343, 1977.
- Kintner, P.M., Jr., Observations of velocity shear driven plasma turbulence, J. Geophys. Res., 81, 5114-5122, 1976.
- Michalke, A., On the inviscid instability of the hyperbolic tangent velocity profile, J. Fluid Mech., 19, 543-556, 1964.
- Mikhailovskii, A.B., Theory of Plasma Instabilities, vol. 2, translated by J.B. Barbour, Consultants Bureau, New York, 1974.
- Mitchell, H.G., M.J. Keskinen, J.A. Fedder, P. Satyanarayana, S.T. Zalesak, and J.D. Huba, Nonlinear evolution of the Kelvin-Helmholtz instability in the high latitude ionosphere, to be submitted to J. Geophys. Res., 1987.
- Miura, A., and T. Sato, Shear instability: auroral deformation and anomalous momentum transport, J. Geophys. Res., 83, 2109-2117, 1978.
- Satyanarayana, P., P. N. Guzdar, J. D. Huba and S. L. Ossakow, Rayleigh-Taylor instability in the presence of a stratified shear layer, J. Geophys. Res., 89, 2945, 1984.
- Sperling, J.L., J.F. Drake, S.T. Zalesak, and J.D. Huba, The role of finite parallel length on the stability of barium clouds, J. Geophys. Res., 89, 10910, 1984.
- Thompson, W.B., Parallel electric fields and shear instabilities, J. Geophys. Res., 88, 4805, 1983.

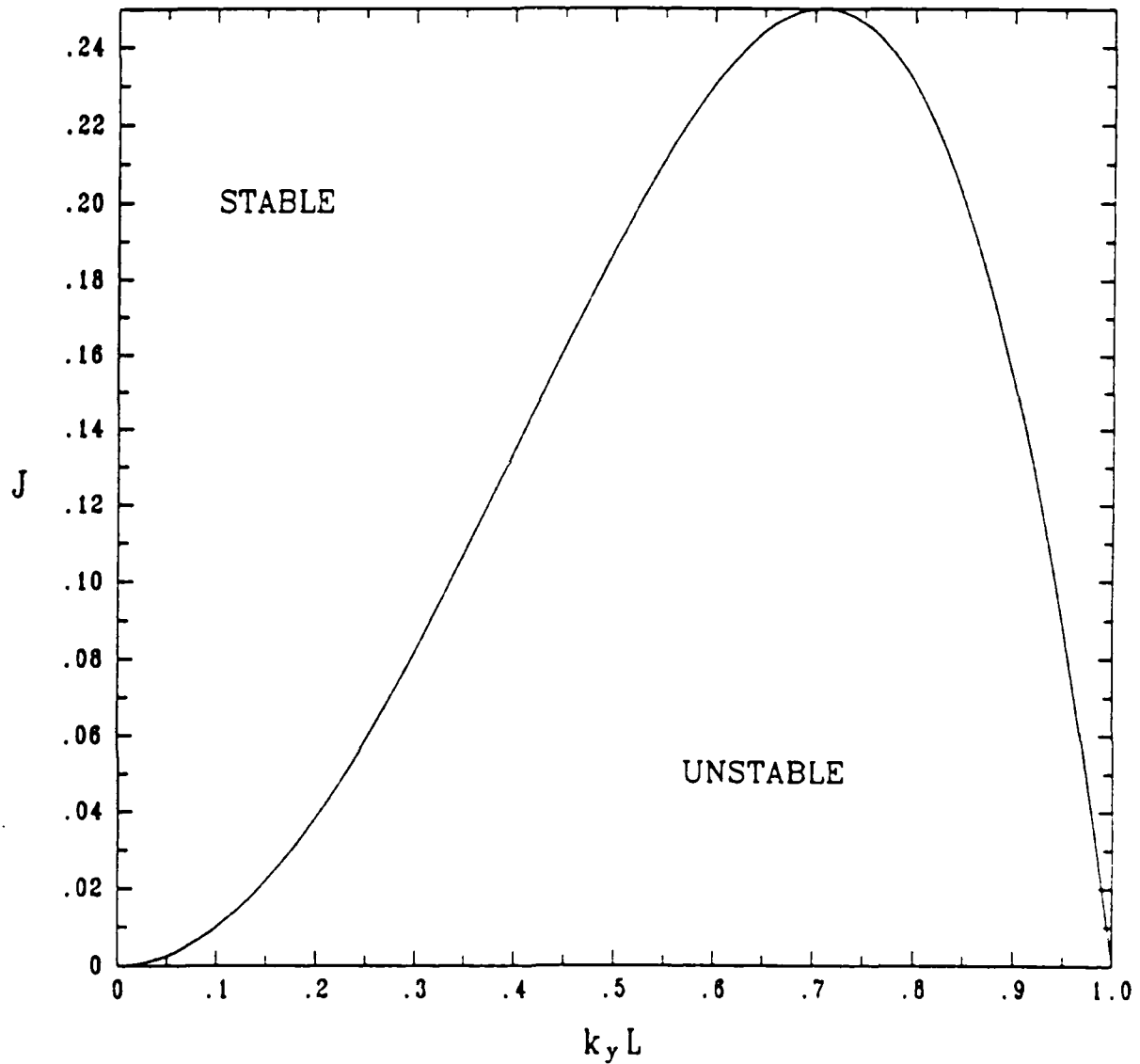


Fig. 1) Stability boundary in the fluid limit. The curve shows the marginal stability boundary ($\gamma = 0$) of $J = (L^2 \omega_{zh}^2 / V_0^2) (k_z^2 / k_y^2)$ vs $k_y L$.

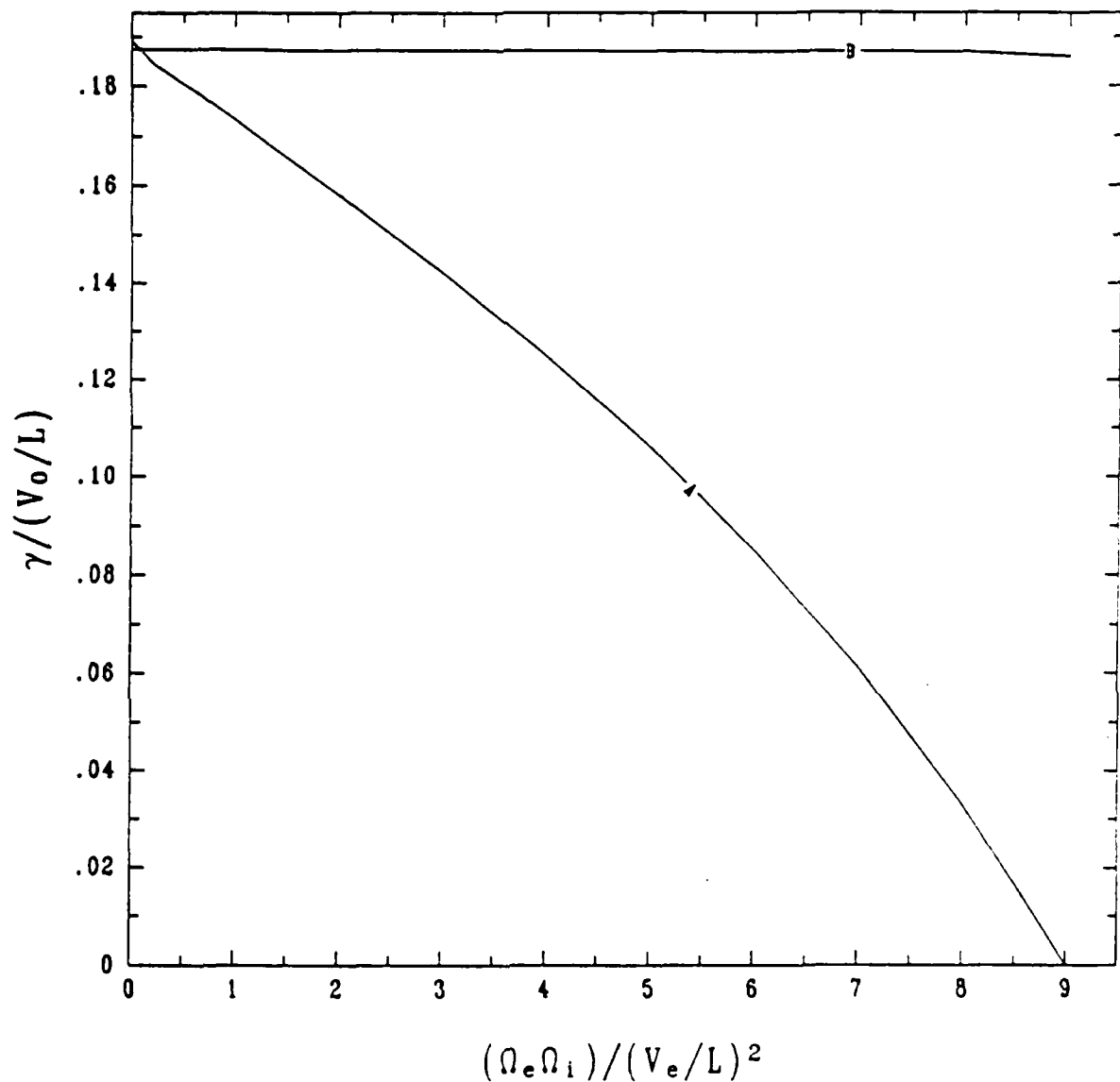


Fig. 2) Plot of the normalized growth rate $\gamma/(V_0/L)$ vs $\alpha (= L^2 \omega_{eh}^2 / v_e^2)$. The parameters used are $k_y L = 0.5$, $k_z / k_y = 1.0 \times 10^{-3}$, $V_0 / v_e = 0.01$, and $V_d = 0$. Curve A is for the collisionless case ($v_e = 0$), while curve B is for the collisional case ($v_e = 100 V_0 / L$).

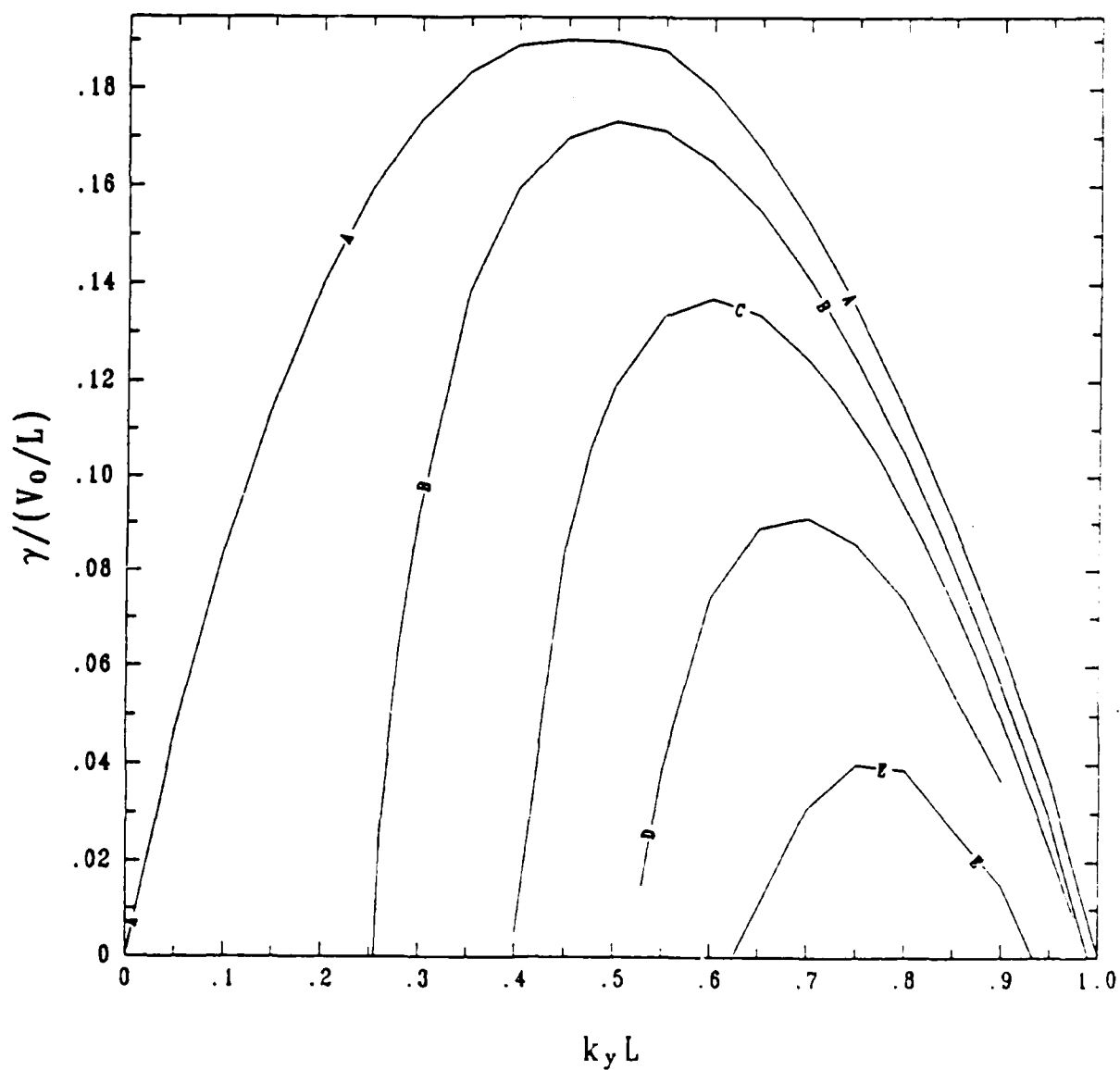


Fig. 3) Plot of the normalized growth rate $\gamma/(V_0/L)$ vs $k_y L$ for $V_0/v_e = 0.01$, $\alpha = 1$, $V_d = 0$ and $k_z L = 0, 1 \times 10^{-3}, 2 \times 10^{-3}$, and 4×10^{-3} , labelled A - E, respectively.

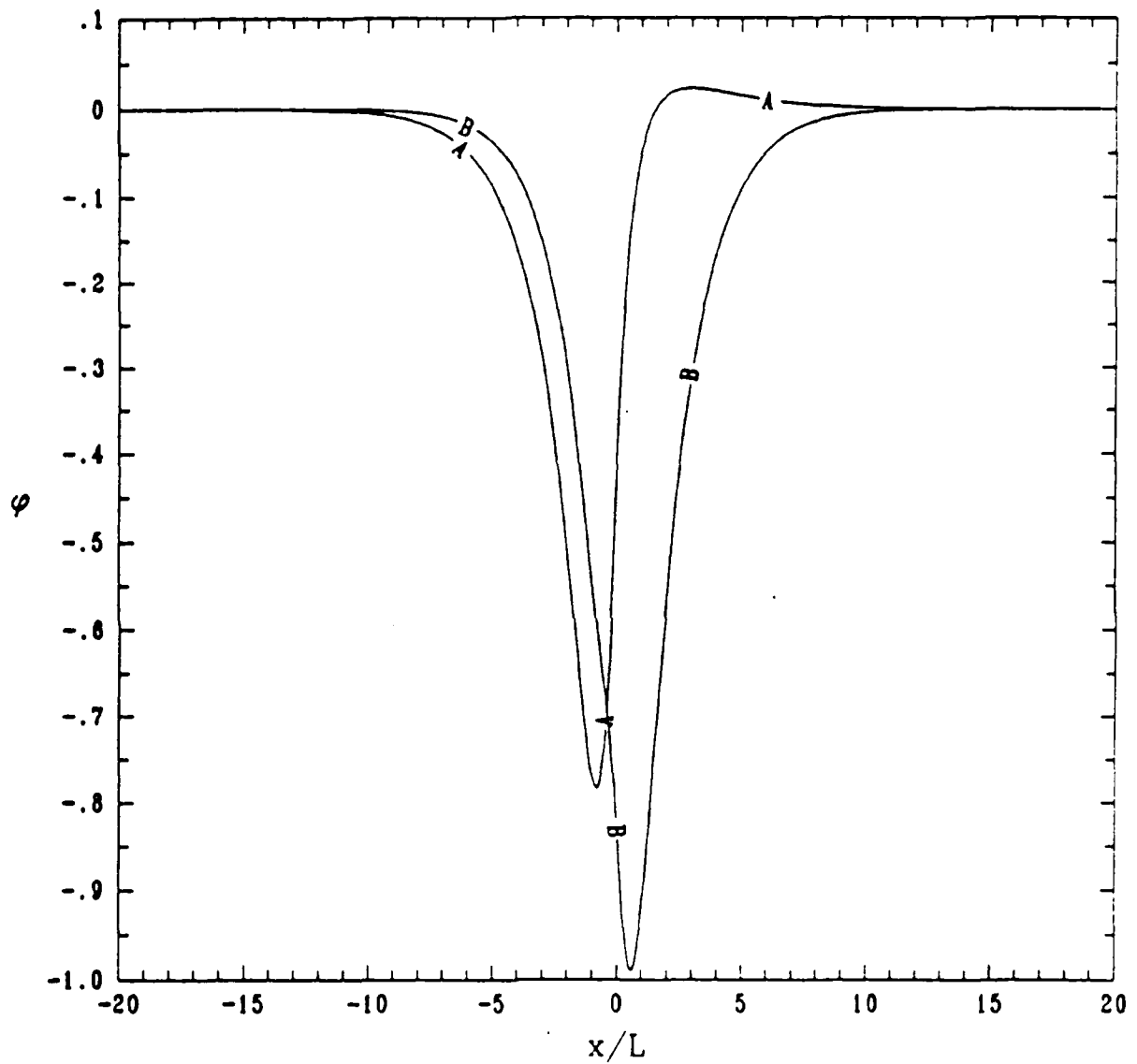


Fig. 4) Eigenfunction for the mode corresponding to curve D of Fig. 3 for $k_y L = 0.7$ ($\gamma = 0.09$). (a) Curves A and B refer to the real and imaginary parts of $\hat{\phi}$, respectively. (b) Contour plots of $\hat{\phi} - \hat{\phi}(x) \exp [ik_y y]$.

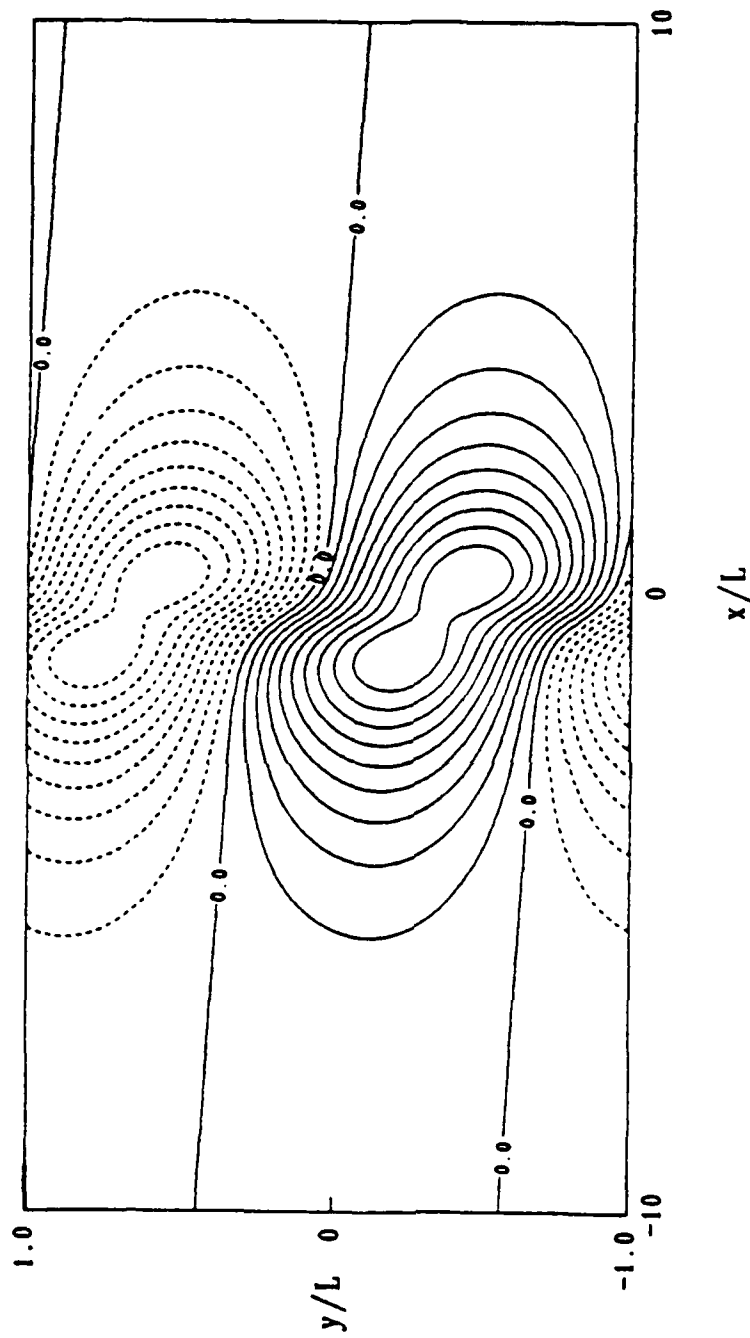


Fig. 4) (Cont) Eigenfunction for the mode corresponding to curve D of Fig. 3 for $k_y L = 0.7$ ($\gamma = 0.09$). (a) Curves A and B refer to the real and imaginary parts of $\hat{\phi}$, respectively. (b) Contour plot of $\hat{\phi} \sim \hat{\phi}(x) \exp [ik_y y]$.

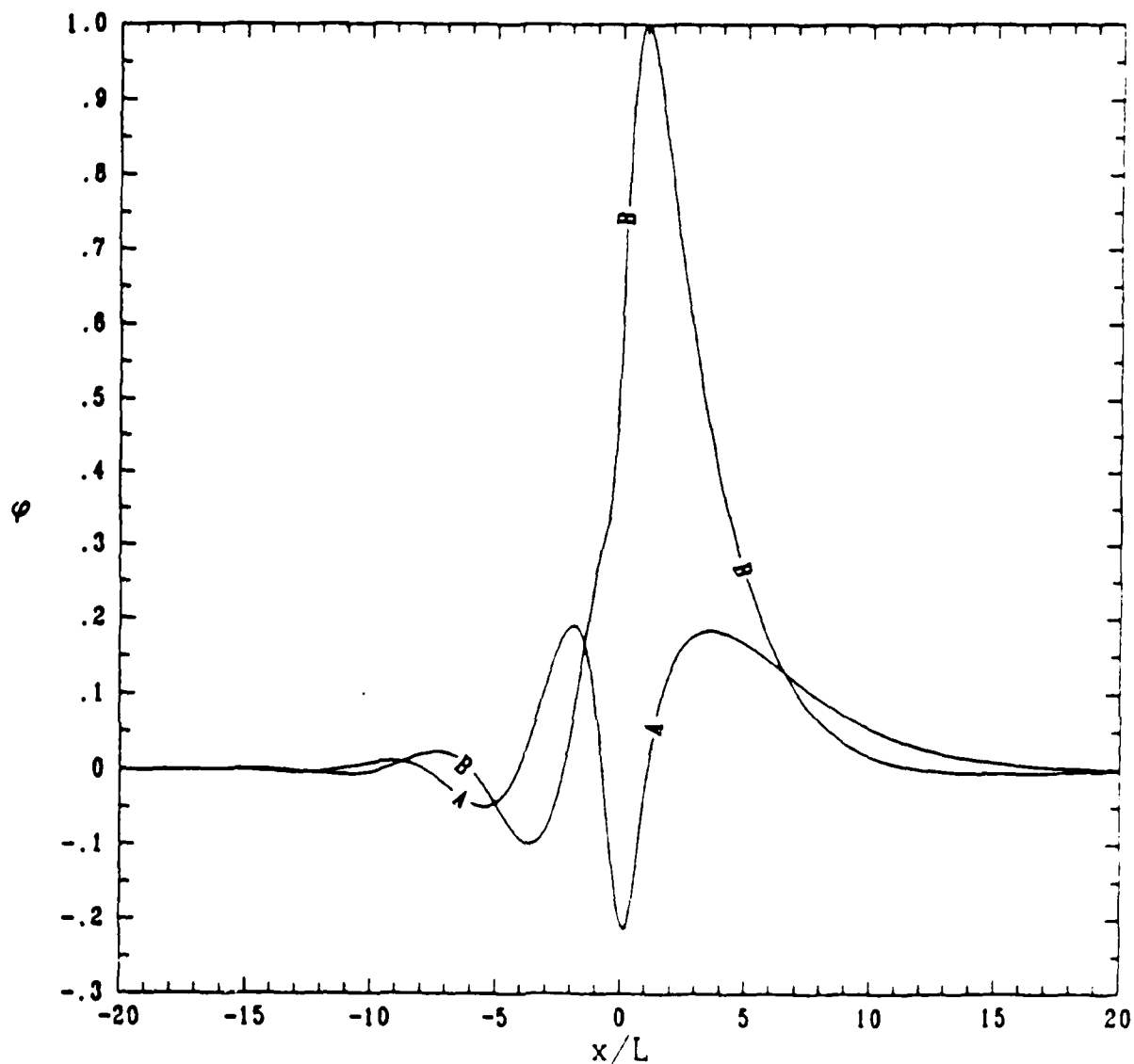


Fig. 5) Eigenfunction for the mode corresponding to Curve D of Fig. 3 for $k_y L = 0.48$ ($\gamma = 0$). (a) Curves A and B refer to the real and imaginary parts of $\hat{\phi}$, respectively. (b) Contour plots of $\hat{\phi} = \hat{\phi}(x) \exp [ik_y y]$.

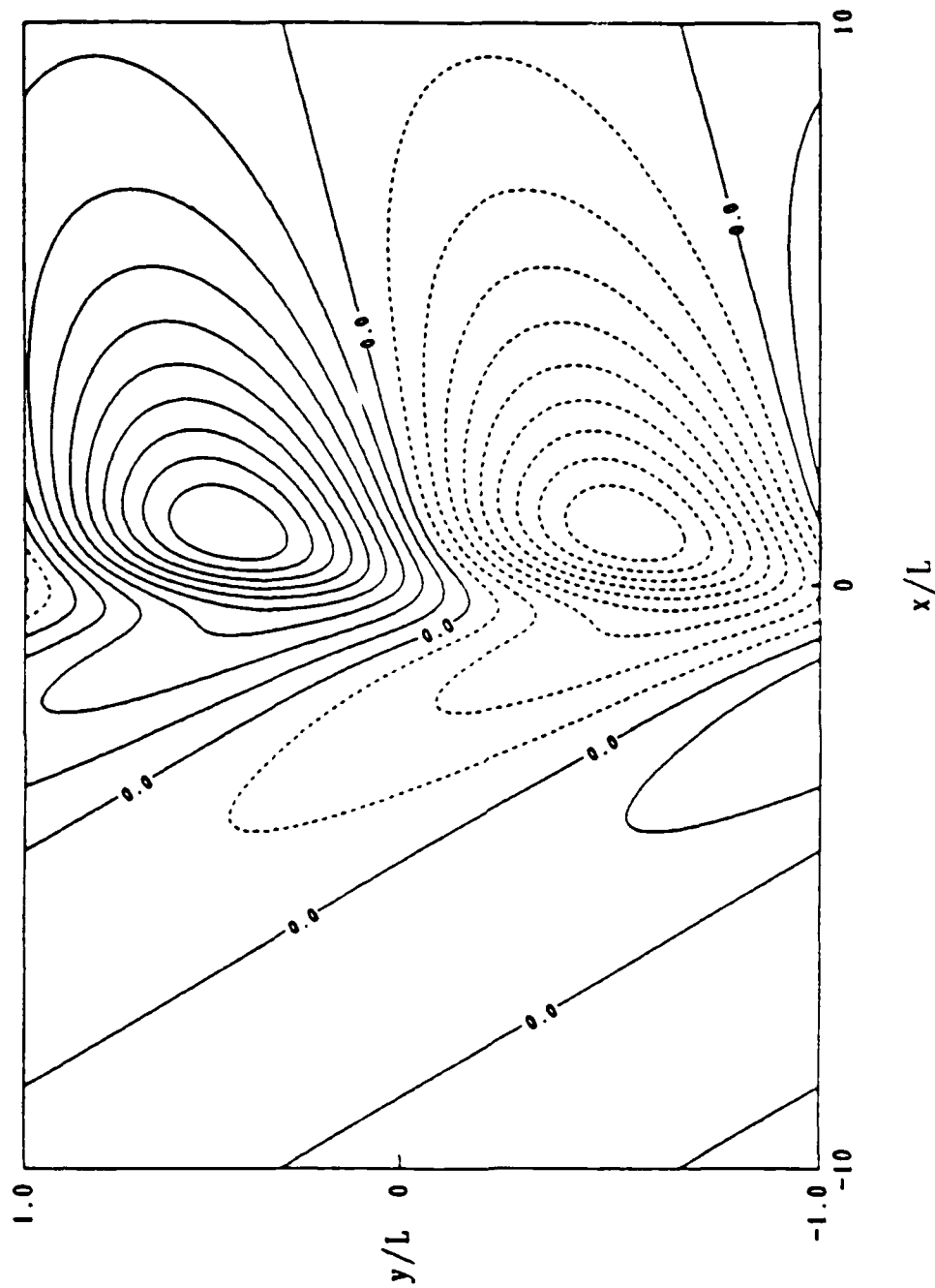


Fig. 5) (Cont) Eigenfunction for the mode corresponding to Curve D of Fig. 3 for $k, L = 0.48$ ($\gamma = 0$). (a) Curves A and B refer to the real and imaginary parts of ϕ , respectively. (b) Contour plots of $\phi = \bar{\phi}(x) \exp [ik_y y]$.

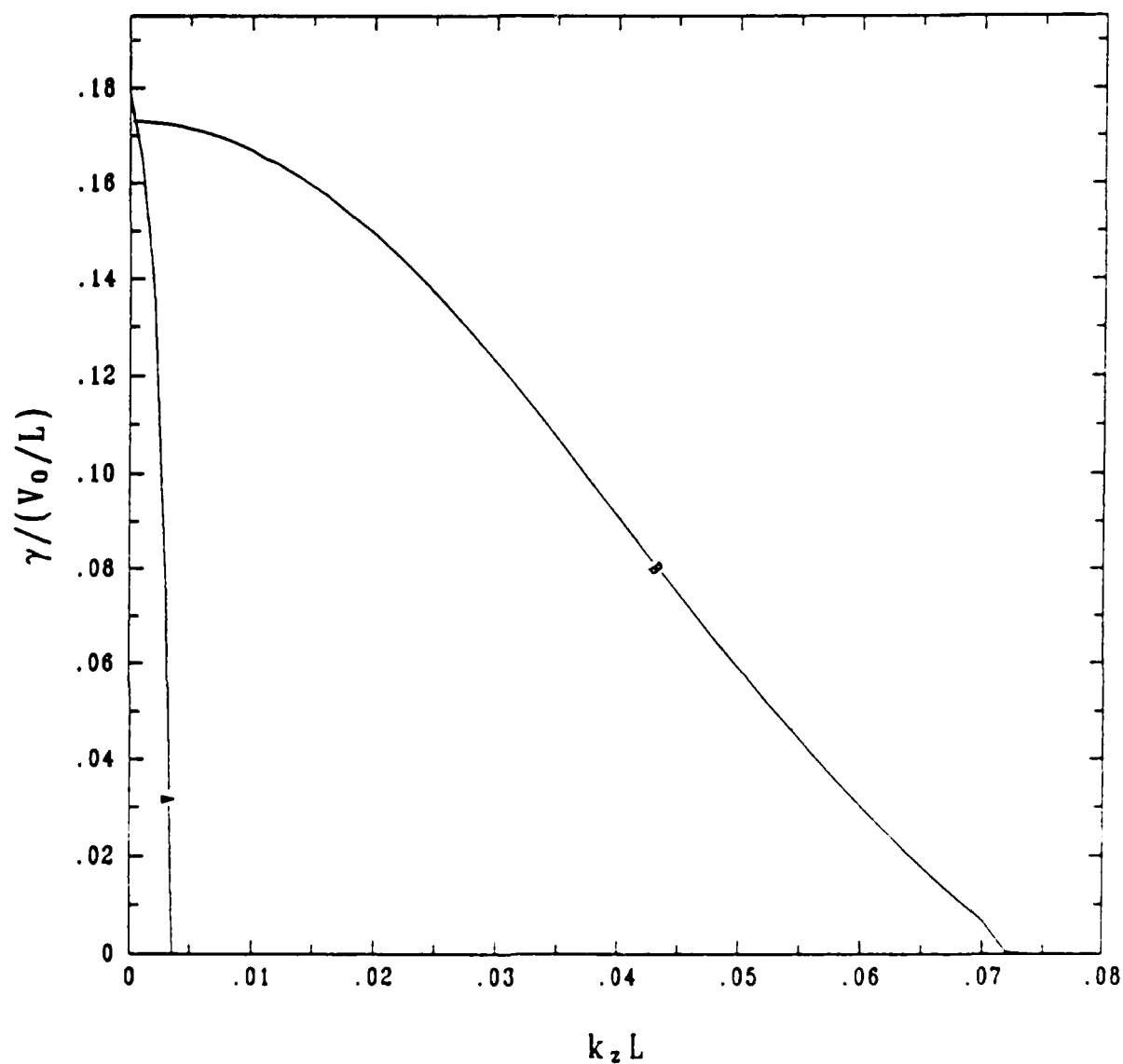


Fig. 6) Plot of the normalized growth rate $\gamma/(V_0/L)$ vs $k_z L$ for $V_d = 0$, $k_y L = 0.5$, $V_0/V_s = 0.01$, and $\alpha = 1$. Curve A corresponds to the case $v_s = 0$ and curve B to $v_s = 100 (V_0/L)$, respectively.

DISTRIBUTION LIST

DEPARTMENT OF DEFENSE

ASSISTANT SECRETARY OF DEFENSE
COMM. CMD, CONT 7 INTELL
WASHINGTON, DC 20301

DIRECTOR
COMMAND CONTROL TECHNICAL CENTER
PENTAGON RM BE 685
WASHINGTON, DC 20301
01CY ATTN C-650
01CY ATTN C-312 R. MASON

DIRECTOR
DEFENSE ADVANCED RSCH PROJ AGENCY
ARCHITECT BUILDING
1400 WILSON BLVD.
ARLINGTON, VA 22209
01CY ATTN NUCLEAR
MONITORING RESEARCH
01CY ATTN STRATEGIC TECH OFFICE

DEFENSE COMMUNICATION ENGINEER CENTER
1860 WIEHLE AVENUE
RESTON, VA 22090
01CY ATTN CODE R410
01CY ATTN CODE R812

DIRECTOR
DEFENSE NUCLEAR AGENCY
WASHINGTON, DC 20305
01CY ATTN STVL
04CY ATTN TITL
01CY ATTN DDST
03CY ATTN RAAE

COMMANDER
FIELD COMMAND
DEFENSE NUCLEAR AGENCY
KIRTLAND, AFB, NM 87115
01CY ATTN FCPR

DEFENSE NUCLEAR AGENCY
SAO/DNA
BUILDING 20676
KIRTLAND AFB, NM 87115
01CY D.C. THORNBURG

DIRECTOR
INTERSERVICE NUCLEAR WEAPONS SCHOOL
KIRTLAND AFB, NM 87115
01CY ATTN DOCUMENT CONTROL

JOINT PROGRAM MANAGEMENT OFFICE
WASHINGTON, DC 20330
01CY ATTN J-3 WWMCCS EVALUATION
OFFICE

DIRECTOR
JOINT STRAT TGT PLANNING STAFF
OFFUTT AFB
OMAHA, NB 68113
01CY ATTN JSTPS/JLKS
01CY ATTN JPST G. GOETZ

CHIEF
LIVERMORE DIVISION FLD COMMAND DNA
DEPARTMENT OF DEFENSE
LAWRENCE LIVERMORE LABORATORY
P.O. BOX 808
LIVERMORE, CA 94550
01CY ATTN FCPRL

COMMANDANT
NATO SCHOOL (SHAPE)
APO NEW YORK 09172
01CY ATTN U.S. DOCUMENTS OFFICER

UNDER SECY OF DEF FOR RSCH & ENGRG
DEPARTMENT OF DEFENSE
WASHINGTON, DC 20301
01CY ATTN STRATEGIC & SPACE
SYSTEMS (OS)

COMMANDER/DIRECTOR
ATMOSPHERIC SCIENCES LABORATORY
U.S. ARMY ELECTRONICS COMMAND
WHITE SANDS MISSILE RANGE, NM 88002
01CY ATTN DELAS-EO, F. NILES

DIRECTOR
BMD ADVANCED TECH CTR
HUNTSVILLE OFFICE
P.O. BOX 1500
HUNTSVILLE, AL 35807
01CY ATTN ATC-T MELVIN T. CAPPS
01CY ATTN ATC-D W. DAVIES
01CY ATTN ATC-R DON RUSC

PROGRAM MANAGER
BMD PROGRAM OFFICE
5001 EISENHOWER AVENUE
ALEXANDRIA, VA 22333
01CY ATTN DACS-BMT J. SHEA

CHIEF C-E- SERVICES DIVISION
U.S. ARMY COMMUNICATIONS CMD
PENTAGON RM 1B269
WASHINGTON, DC 20310
01CY ATTN C- E-SERVICES DIVISION

COMMANDER
U.S. ARMY COMM-ELEC ENGRG INSTAL AGY
FT. HUACHUCA, AZ 85613
01CY ATTN CCC-EMEO GEORGE LANE

COMMANDER
U.S. ARMY FOREIGN SCIENCE & TECH CTR
220 7TH STREET, NE
CHARLOTTESVILLE, VA 22901
01CY ATTN DRXST-SD

COMMANDER
U.S. ARMY MATERIAL DEV & READINESS CMD
5001 EISENHOWER AVENUE
ALEXANDRIA, VA 22333
01CY ATTN DRCLDC J.A. BENDER

COMMANDER
U.S. ARMY NUCLEAR AND CHEMICAL AGENCY
7500 BACKLICK ROAD
BLDG 2073
SPRINGFIELD, VA 22150
01CY ATTN LIBRARY

DIRECTOR
U.S. ARMY BALLISTIC RESEARCH
LABORATORY
ABERDEEN PROVING GROUND, MD 21005
01CY ATTN TECH LIBRARY,
EDWARD BAICY

COMMANDER
U.S. ARMY SATCOM AGENCY
FT. MONMOUTH, NJ 07703
01CY ATTN DOCUMENT CONTROL

COMMANDER
U.S. ARMY MISSILE INTELLIGENCE AGENCY
REDSTONE ARSENAL, AL 35809
01CY ATTN JIM GAMBLE

DIRECTOR
U.S. ARMY TRADOC SYSTEMS ANALYSIS
ACTIVITY
WHITE SANDS MISSILE RANGE, NM 88002
01CY ATTN ATAA-SA
01CY ATTN TCC/F. PAYAN JR.
01CY ATTN ATTA-TAC LTC J. HESSE

COMMANDER
NAVAL ELECTRONIC SYSTEMS COMMAND
WASHINGTON, DC 20360
01CY ATTN NAVALEX 034 T. HUGHES
01CY ATTN PME 117
01CY ATTN PME 117-T
01CY ATTN CODE 5011

COMMANDING OFFICER
NAVAL INTELLIGENCE SUPPORT CTR
4301 SUITLAND ROAD, BLDG. 5
WASHINGTON, DC 20390
01CY ATTN MR. DUBBIN STIC 12
01CY ATTN NISC-50
01CY ATTN CODE 5404 J. GALET

COMMANDER
NAVAL OCEAN SYSTEMS CENTER
SAN DIEGO, CA 92152
01CY ATTN J. FERGUSON

NAVAL RESEARCH LABORATORY
WASHINGTON, DC 20375
01CY ATTN CODE 4700 S.L. Ossakow,
26 CYS IF UNCLASS
(01CY IF CLASS)
ATTN CODE 4780 J.D. HUBA, 50
CYS IF UNCLASS, 01CY IF CLAS
01CY ATTN CODE 4701 I. VITKOVITSK
01CY ATTN CODE 7500
01CY ATTN CODE 7550
01CY ATTN CODE 7580
01CY ATTN CODE 7551
01CY ATTN CODE 7555
01CY ATTN CODE 4730 E. MCLEAN
01CY ATTN CODE 4752
01CY ATTN CODE 4730 B. RIPIN
20CY ATTN CODE 2628

COMMANDER
NAVAL SPACE SURVEILLANCE SYSTEM
DAHLGREN, VA 22448
01CY ATTN CAPT J.H. BURTON

OFFICER-IN-CHARGE
NAVAL SURFACE WEAPONS CENTER
WHITE OAK, SILVER SPRING, MD 20910
01CY ATTN CODE F31

DIRECTOR
STRATEGIC SYSTEMS PROJECT OFFICE
DEPARTMENT OF THE NAVY
WASHINGTON, DC 20376
01CY ATTN NSP-2141
01CY ATTN NSSP-2722 FRED WIMBERLY

COMMANDER
NAVAL SURFACE WEAPONS CENTER
DAHLGREN LABORATORY
DAHLGREN, VA 22448
01CY ATTN CODE DF-14 R. BUTLER

OFFICER OF NAVAL RESEARCH
ARLINGTON, VA 22217
01CY ATTN CODE 465
01CY ATTN CODE 461
01CY ATTN CODE 402
01CY ATTN CODE 420
01CY ATTN CODE 421

COMMANDER
AEROSPACE DEFENSE COMMAND/XPD
DEPARTMENT OF THE AIR FORCE
ENT AFB, CO 80912
01CY ATTN XPDQQ
01CY ATTN XP

AIR FORCE GEOPHYSICS LABORATORY
HANSCOM AFB, MA 01731
01CY ATTN OPR HAROLD GARDNER
01CY ATTN LKB
KENNETH S.W. CHAMPION
01CY ATTN OPR ALVA T. STAIR
01CY ATTN PHD JURGEN BUCHAU
01CY ATTN PHD JOHN P. MULLEN

AF WEAPONS LABORATORY
KIRTLAND AFB, NM 87117
01CY ATTN SUL
01CY ATTN CA ARTHUR H. GUENTHER
01CY ATTN NTYCE 1LT. G. KRAJEI

AFTAC
PATRICK AFB, FL 32925
01CY ATTN TN

AIR FORCE AVIONICS LABORATORY
WRIGHT-PATTERSON AFB, OH 45433
01CY ATTN AAD WADE HUNT
01CY ATTN AAD ALLEN JOHNSON

DEPUTY CHIEF OF STAFF
RESEARCH, DEVELOPMENT, & ACQ
DEPARTMENT OF THE AIR FORCE
WASHINGTON, DC 20330
01CY ATTN AFRDQ

HEADQUARTERS
ELECTRONIC SYSTEMS DIVISION
DEPARTMENT OF THE AIR FORCE
HANSCOM AFB, MA 01731-5000
01CY ATTN J. DEAS
ESD/SCD-4

COMMANDER
FOREIGN TECHNOLOGY DIVISION, AFSC
WRIGHT-PATTERSON AFB, OH 45433
01CY ATTN NICD LIBRARY
01CY ATTN ETD P. B. BALLARD

COMMANDER
ROME AIR DEVELOPMENT CENTER, AFSC
GRIFFISS AFB, NY 13441
01CY ATTN DOC LIBRARY/TSLO
01CY ATTN OCSE V. COYNE

STRATEGIC AIR COMMAND/XPFS
OFFUTT AFB, NE 68113
01CY ATTN XPFS

SAMSO/MN
NORTON AFB, CA 92409
(MINUTEMAN)
01CY ATTN MNNL

COMMANDER
ROME AIR DEVELOPMENT CENTER, AFSC
HANSCOM AFB, MA 01731
01CY ATTN EEP A. LORENTZEN

DEPARTMENT OF ENERGY
LIBRARY ROOM G-042
WASHINGTON, DC 20545
01CY ATTN DOC CON FOR A. LABOWITZ

DEPARTMENT OF ENERGY
ALBUQUERQUE OPERATIONS OFFICE
P.O. BOX 5400
ALBUQUERQUE, NM 87115
01CY ATTN DOC CON FOR D. SHERWOOD

SG&G, INC.
LOS ALAMOS DIVISION
P.O. BOX 809
LOS ALAMOS, NM 85544
01CY ATTN DOC CON FOR J. BREEDLOVE

UNIVERSITY OF CALIFORNIA
LAWRENCE LIVERMORE LABORATORY
P.O. BOX 808
LIVERMORE, CA 94550
01CY ATTN DOC CON FOR TECH INFO
DEPT
01CY ATTN DOC CON FOR L-389 R. OTT
01CY ATTN DOC CON FOR L-31 R. HAGER

LOS ALAMOS NATIONAL LABORATORY
P.O. BOX 1663
LOS ALAMOS, NM 87545
01CY ATTN DOC CON FOR J. WOLCOTT
01CY ATTN DOC CON FOR R.F. TASCHEK
01CY ATTN DOC CON FOR E. JONES
01CY ATTN DOC CON FOR J. MALIK
01CY ATTN DOC CON FOR R. JEFFRIES
01CY ATTN DOC CON FOR J. ZINN
01CY ATTN DOC CON FOR D. WESTERVELT
01CY ATTN D. SAPPENFIELD

LOS ALAMOS NATIONAL LABORATORY
MS D438
LOS ALAMOS, NM 87545
01CY ATTN S.P. GARY
01CY ATTN J. BOROVSKY

SANDIA LABORATORIES
P.O. BOX 5800
ALBUQUERQUE, NM 87115
01CY ATTN DOC CON FOR W. BROWN
01CY ATTN DOC CON FOR A.
THORNBROUGH
01CY ATTN DOC CON FOR T. WRIGHT
01CY ATTN DOC CON FOR D. DAHLGREN
01CY ATTN DOC CON FOR 3141
01CY ATTN DOC CON FOR SPACE PROJECT
DIV

SANDIA LABORATORIES
LIVERMORE LABORATORY
P.O. BOX 969
LIVERMORE, CA 94550
01CY ATTN DOC CON FOR B. MURPHEY
01CY ATTN DOC CON FOR T. COOK

OFFICE OF MILITARY APPLICATION
DEPARTMENT OF ENERGY
WASHINGTON, DC 20545
01CY ATTN DOC CON DR. YO SONG

NATIONAL OCEANIC & ATMOSPHERIC ADMIN
ENVIRONMENTAL RESEARCH LABORATORIES
DEPARTMENT OF COMMERCE
BOULDER, CO 80302
01CY ATTN R. GRUBB

DEPARTMENT OF DEFENSE CONTRACTORS

AEROSPACE CORPORATION
P.O. BOX 92957
LOS ANGELES, CA 90009
01CY ATTN I. GARFUNKEL
01CY ATTN T. SALMI
01CY ATTN V. JOSEPHSON
01CY ATTN S. BOWER
01CY ATTN D. OLSEN

ANALYTICAL SYSTEMS ENGINEERING CORP
5 OLD CONCORD ROAD
BURLINGTON, MA 01803
01CY ATTN RADIO SCIENCES

AUSTIN RESEARCH ASSOC., INC.
1901 RUTLAND DRIVE
AUSTIN, TX 78758
01CY ATTN L. SLOAN
01CY ATTN R. THOMPSON.

BERKELEY RESEARCH ASSOCIATES, INC.
P.O. BOX 983
BERKELEY, CA 94701
01CY ATTN J. WORKMAN
01CY ATTN C. PRETTIE
01CY ATTN S. BRECHT

BOEING COMPANY, THE
P.O. BOX 3707
SEATTLE, WA 98124
01CY ATTN G. KEISTER
01CY ATTN D. MURRAY
01CY ATTN G. HALL
01CY ATTN J. KENNEY

CHARLES STARK DRAPER LABORATORY, INC.
555 TECHNOLOGY SQUARE
CAMBRIDGE, MA 02139
01CY ATTN D.B. COX
01CY ATTN J.P. GILMORE

COMSAT LABORATORIES
22300 COMSAT DRIVE
CLARKSBURG, MD 20871
01CY ATTN G. HYDE

CORNELL UNIVERSITY
DEPARTMENT OF ELECTRICAL ENGINEERING
ITHACA, NY 14850
01CY ATTN D.T. FARLEY, JR.

ELECTROSPACE SYSTEMS, INC.
BOX 1359
RICHARDSON, TX 75080
01CY ATTN H. LOGSTON
01CY ATTN SECURITY (PAUL PHILLIPS)

EOS TECHNOLOGIES, INC.
606 Wilshire Blvd.
Santa Monica, CA 90401
01CY ATTN C.B. GABBARD
01CY ATTN R. LELEVIER

GENERAL ELECTRIC COMPANY
SPACE DIVISION
VALLEY FORGE SPACE CENTER
GODDARD BLVD KING OF PRUSSIA
P.O. BOX 8555
PHILADELPHIA, PA 19101
01CY ATTN M.H. BORTNER
SPACE SCI LAB

GENERAL ELECTRIC TECH SERVICES
CO., INC.
HMES
COURT STREET
SYRACUSE, NY 13201
01CY ATTN G. MILLMAN

GEOPHYSICAL INSTITUTE
UNIVERSITY OF ALASKA
FAIRBANKS, AK 99701
(ALL CLASS ATTN: SECURITY OFFICER)
01CY ATTN T.N. DAVIS (UNCLASS ONLY)
01CY ATTN NEAL BROWN (UNCLASS ONLY)

GTE SYLVANIA, INC.
ELECTRONICS SYSTEMS GRP-EASTERN DIV
77 A STREET
NEEDHAM, MA 02194
01CY ATTN DICK STEINHOF

HSS, INC.
2 ALFRED CIRCLE
BEDFORD, MA 01730
01CY ATTN DONALD HANSEN

ILLINOIS, UNIVERSITY OF
107 COBLE HALL
150 DAVENPORT HOUSE
CHAMPAIGN, IL 61820
(ALL CORRES ATTN DAN MCCLELLAND)
01CY ATTN K. YEH

INSTITUTE FOR DEFENSE ANALYSES
1801 NO. BEAUREGARD STREET
ALEXANDRIA, VA 22311
01CY ATTN J.M. AEIN
01CY ATTN ERNEST BAUER
01CY ATTN HANS WOLFARD
01CY ATTN JOEL BENGSTON

INTL TEL & TELEGRAPH CORPORATION
500 WASHINGTON AVENUE
MUTLEY, NJ 07110
01CY ATTN TECHNICAL LIBRARY

JAYCOR
11011 TORREYANA ROAD
P.O. BOX 85154
SAN DIEGO, CA 92138
01CY ATTN J.L. SPERLING

JOHNS HOPKINS UNIVERSITY
APPLIED PHYSICS LABORATORY
JOHNS HOPKINS ROAD
LAUREL, MD 20810
01CY ATTN DOCUMENT LIBRARIAN
01CY ATTN THOMAS POTEIRA
01CY ATTN JOHN DASSOULAS

KAMAN SCIENCES CORP
P.O. BOX 7463
COLORADO SPRINGS, CO 80933
01CY ATTN T. MEAGHER

KAMAN TEMPO-CENTER FOR ADVANCED
STUDIES
816 STATE STREET (P.O. DRAWER QQ)
SANTA BARBARA, CA 93102
01CY ATTN DASIAC
01CY ATTN WARREN S. KNAPP
01CY ATTN WILLIAM MCNAMARA
01CY ATTN B. GAMBILL

LINKABIT CORP
10453 ROSELLE
SAN DIEGO, CA 92121
01CY ATTN IRWIN JACOBS

LOCKHEED MISSILES & SPACE CO., INC
P.O. BOX 504
SUNNYVALE, CA 94088
01CY ATTN DEPT 60-12
01CY ATTN D.R. CHURCHILL

LOCKHEED MISSILES & SPACE CO., INC.
3251 HANOVER STREET
PALO ALTO, CA 94304
01CY ATTN MARTIN WALT DEPT 52-12
01CY ATTN W.L. IMHOF DEPT 52-12
01CY ATTN RICHARD G. JOHNSON
DEPT 52-12
01CY ATTN J.B. CLADIS DEPT 52-12

MARTIN MARIETTA CORP
ORLANDO DIVISION
P.O. BOX 5837
ORLANDO, FL 32805
01CY ATTN R. HEFFNER

MCDONNELL DOUGLAS CORPORATION
5301 BOLSA AVENUE
HUNTINGTON BEACH, CA 92647
01CY ATTN N. HARRIS
01CY ATTN J. MOULE
01CY ATTN GEORGE MROZ
01CY ATTN W. OLSON
01CY ATTN R.W. HALPRIN
01CY ATTN TECHNICAL
LIBRARY SERVICES

MISSION RESEARCH CORPORATION
735 STATE STREET
SANTA BARBARA, CA 93101
01CY ATTN P. FISCHER
01CY ATTN W.F. CREVIER
01CY ATTN STEVEN L. GUTSCHE
01CY ATTN R. BOGUSCH
01CY ATTN R. HENDRICK
01CY ATTN RALPH KILB
01CY ATTN DAVE SOWLE
01CY ATTN F. FAJEN
01CY ATTN M. SCHEIBE
01CY ATTN CONRAD L. LONGMIRE
01CY ATTN B. WHITE
01CY ATTN R. STAGAT

MISSION RESEARCH CORP.
1720 RANDOLPH ROAD, S.E.
ALBUQUERQUE, NM 87106
01CY R. STELLINGWERF
01CY M. ALME
01CY L. WRIGHT

MITRE CORP
WESTGATE RESEARCH PARK
1820 DOLLY MADISON BLVD
MCLEAN, VA 22101
01CY ATTN W. HALL
01CY ATTN W. FOSTER

PACIFIC-SIERRA RESEARCH CORP
12340 SANTA MONICA BLVD.
LOS ANGELES, CA 90025
01CY ATTN E.C. FIELD, JR.

PENNSYLVANIA STATE UNIVERSITY
IONOSPHERE RESEARCH LAB
318 ELECTRICAL ENGINEERING EAST
UNIVERSITY PARK, PA 16802
(NO CLASS TO THIS ADDRESS)
01CY ATTN IONOSPHERIC RESEARCH LAB

PHOTOMETRICS, INC.
4 ARROW DRIVE
WOBBURN, MA 01801
01CY ATTN IRVING L. KOFSKY

PHYSICAL DYNAMICS, INC.
P.O. BOX 3027
BELLEVUE, WA 98009
01CY ATTN E.J. FREMOUW

PHYSICAL DYNAMICS, INC.
P.O. BOX 10367
OAKLAND, CA 94610
ATTN A. THOMSON

R & D ASSOCIATES
P.O. BOX 9695
MARINA DEL REY, CA 90291
01CY ATTN FORREST GILMORE
01CY ATTN WILLIAM B. WRIGHT, JR.
01CY ATTN WILLIAM J. KARZAS
01CY ATTN H. ORY
01CY ATTN C. MACDONALD
01CY ATTN BRIAN LAMB
01CY ATTN MORGAN GROVER

RAYTHEON CO.
528 BOSTON POST ROAD
SUDBURY, MA 01776
01CY ATTN BARBARA ADAMS

RIVERSIDE RESEARCH INSTITUTE
330 WEST 42nd STREET
NEW YORK, NY 10036
01CY ATTN VINCE TRAPANI

SCIENCE APPLICATIONS
INTERNATIONAL INCORPORATED
1150 PROSPECT PLAZA
LA JOLLA, CA 92037
01CY ATTN LEWIS M. LINSON
01CY ATTN DANIEL A. HAMLIN
01CY ATTN E. FRIEMAN
01CY ATTN E.A. STRAKER
01CY ATTN CURTIS A. SMITH

SCIENCE APPLICATIONS
INTERNATIONAL CORPORATION
1710 GOODRIDGE DR.
MCLEAN, VA 22102
01CY J. COCKAYNE
01CY E. HYMAN

SRI INTERNATIONAL
333 RAVENSWOOD AVENUE
MENLO PARK, CA 94025
01CY ATTN J. CASPER
01CY ATTN DONALD NEILSON
01CY ATTN ALAN BURNS
01CY ATTN G. SMITH
01CY ATTN R. TSUNODA
01CY ATTN DAVID A. JOHNSON
01CY ATTN WALTER G. CHESNUT
01CY ATTN CHARLES L. RINO
01CY ATTN WALTER JAYE
01CY ATTN J. VICKREY
01CY ATTN RAY L. LEADABRAND
01CY ATTN G. CARPENTER
01CY ATTN G. PRICE
01CY ATTN R. LIVINGSTON
01CY ATTN V. GONZALES
01CY ATTN D. MCDANIEL

TECHNOLOGY INTERNATIONAL CORP
75 WIGGINS AVENUE
BEDFORD, MA 01730
01CY ATTN W.P. BOQUIST

TRW DEFENSE & SPACE SYS GROUP
ONE SPACE PARK
REDONDO BEACH, CA 90278
01CY ATTN R. K. PLEBUCH
01CY ATTN S. ALTSCHULER
01CY ATTN D. DEE
01CY ATTN D/ STOCKWELL
SNTF/1575

VISIDYNE
SOUTH BEDFORD STREET
BURLINGTON, MA 01803
01CY ATTN W. REIDY
01CY ATTN J. CARPENTER
01CY ATTN C. HUMPHREY

UNIVERSITY OF PITTSBURGH
PITTSBURGH, PA 15213
01CY ATTN: N. ZABUSKY

IONOSPHERIC MODELING DISTRIBUTION LIST
(UNCLASSIFIED ONLY)

PLEASE DISTRIBUTE ONE COPY TO EACH OF THE FOLLOWING PEOPLE (UNLESS OTHERWISE NOTED)

NAVAL RESEARCH LABORATORY

WASHINGTON, DC 20375
DR. H. GURSKY - CODE 4100
DR. J.M. GOODMAN - CODE 4180
DR. P. RODRIGUEZ - CODE 4750
DR. P. MANGE - CODE 4101
DR. R. MEIER - CODE 4140
CODE 2628 (22 COPIES)
CODE 1220

A.F. GEOPHYSICS LABORATORY

L.G. HANSCOM FIELD
BEDFORD, MA 01731
DR. T. ELKINS
DR. W. SWIDER
MRS. R. SAGALYN
DR. J.M. FORBES
DR. T.J. KENESHEA
DR. W. BURKE
DR. H. CARLSON
DR. J. JASPERSE
DR. F.J. RICH
DR. N. MAYNARD
DR. D.N. ANDERSON
DR. S. BASU

BOSTON UNIVERSITY
DEPARTMENT OF ASTRONOMY
BOSTON, MA 02215

DR. J. AARONS
DR. M. MENDILLO

CORNELL UNIVERSITY

ITHACA, NY 14850
DR. B. FEJER
DR. R. SUDAN
DR. D. FARLEY
DR. M. KELLEY

HARVARD UNIVERSITY

HARVARD SQUARE
CAMBRIDGE, MA 02138
DR. M.B. McELROY

INSTITUTE FOR DEFENSE ANALYSIS

1801 N. BEAUREGARD STREET
ARLINGTON, VA 22311
DR. E. BAUER

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

PLASMA FUSION CENTER
CAMBRIDGE, MA 02139
LIBRARY, NW16-262
DR. T. CHANG
DR. R. LINDZEN

NASA

GODDARD SPACE FLIGHT CENTER
GREENBELT, MD 20771
DR. N. MAYNARD (CODE 696)
DR. R.F. BENSON
DR. K. MAEDA
DR. S. CURTIS
DR. M. DUBIN

COMMANDER

NAVAL AIR SYSTEMS COMMAND
DEPARTMENT OF THE NAVY
WASHINGTON, DC 20360
DR. T. CZUBA

COMMANDER

NAVAL OCEAN SYSTEMS CENTER
SAN DIEGO, CA 92152
MR. R. ROSE - CODE 5321

NOAA

DIRECTOR OF SPACE AND ENVIRONMENTAL
LABORATORY
BOULDER, CO 80302
DR. A. GLENN JEAN
DR. G.W. ADAMS
DR. K. DAVIES
DR. R. F. DONNELLY

OFFICE OF NAVAL RESEARCH

800 NORTH QUINCY STREET
ARLINGTON, VA 22217
DR. G. JOINER

LABORATORY FOR PLASMA AND

FUSION ENERGIES STUDIES
UNIVERSITY OF MARYLAND
COLLEGE PARK, MD 20742
JHAN VARYAN HELLMAN,
REFERENCE LIBRARIAN

PENNSYLVANIA STATE UNIVERSITY
UNIVERSITY PARK, PA 16802

DR. J.S. NISBET
DR. P.R. ROHRBAUGH
DR. L.A. CARPENTER
DR. M. LEE
DR. R. DIVANY
DR. P. BENNETT
DR. E. KLEVANS

PRINCETON UNIVERSITY
PLASMA PHYSICS LABORATORY
PRINCETON, NJ 08540
DR. F. PERKINS

SAIC
1150 PROSPECT PLAZA
LA JOLLA, CA 92037
DR. D.A. HAMLIN
DR. L. LINSON
DR. E. FRIEMAN

SRI INTERNATIONAL
333 RAVENSWOOD AVENUE
MENLO PARK, CA 94025
DR. R. TSUNODA
DR. WALTER G. CHESNUT
DR. CHARLES L. RING
DR. J. VICKREY
DR. R. LIVINGSTON

STANFORD UNIVERSITY
STANFORD, CA 94305
DR. P.M. BANKS
DR. R. HELLIWELL

U.S. ARMY ABERDEEN RESEARCH
AND DEVELOPMENT CENTER
BALLISTIC RESEARCH LABORATORY
ABERDEEN, MD
DR. J. HEIMERL

GEOPHYSICAL INSTITUTE
UNIVERSITY OF ALASKA
FAIRBANKS, AK 99701
DR. L.C. LEE

UTAH STATE UNIVERSITY
4TH AND 8TH STREETS
LOGAN, UT 84322
DR. R. HARRIS
DR. K. BAKER
DR. R. SCHUNK
DR. J. ST.-MAURICE
DR. N. SINGH

UNIVERSITY OF CALIFORNIA
LOS ALAMOS NATIONAL LABORATORY
ESS DIVISION
LOS ALAMOS, NM 87545
DR. M. PONGRATZ, ESS-DOT
DR. D. SIMONS, ESS-7, MS-D466
DR. L. DUNCAN, ESS-7, MS-D466
DR. P. BERNHARDT, ESS-7, MS-D466
DR. S.P. GARY, ESS-3

UNIVERSITY OF ILLINOIS
DEPT. OF ELECTRICAL ENGINEERING
1406 W. GREEN STREET
URBANA, IL 61801
DR. ERHAN KUDEKI

UNIVERSITY OF CALIFORNIA,
LOS ANGELES
405 HILLCARD AVENUE
LOS ANGELES, CA 90024
DR. F.V. CORONITI
DR. C. KENNEL
DR. A.Y. WONG

UNIVERSITY OF MARYLAND
COLLEGE PARK, MD 20740
DR. K. PAPADOPOULOS
DR. E. OTT

JOHNS HOPKINS UNIVERSITY
APPLIED PHYSICS LABORATORY
JOHNS HOPKINS ROAD
LAUREL, MD 20810
DR. R. GREENWALD
DR. C. MENG
DR. T. POTEMRA

UNIVERSITY OF PITTSBURGH
PITTSBURGH, PA 15213
DR. N. ZABUSKY
DR. M. BIGNOI
DR. E. OVERMAN

UNIVERSITY OF TEXAS
AT DALLAS
CENTER FOR SPACE SCIENCES
P.O. BOX 688
RICHARDSON, TX 75080
DR. R. HEELIS
DR. W. HANSON
DR. J.P. MACLURE

DIRECTOR OF RESEARCH
U.S. NAVAL ACADEMY
ANNAPOLIS, MD 21402
(2 COPIES)

END

7-87

DTIC